

EVOLUTION OF GALACTIC OUTFLOWS AT $z \sim 0$ –2 REVEALED WITH SDSS, DEEP2, AND KECK SPECTRA

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ABSTRACT

We study galactic outflows of star-forming galaxies at $z \sim 0$ –2 based on optical spectra with absorption lines of Na I D, Mg I, Mg II, C II, and C IV. The spectra of galaxies at $z \sim 0$, 1, and 2 are taken from the large-survey data sets of SDSS DR7, DEEP2 DR4, and [Erb et al. \(2006a,b\)](#), respectively. To remove possible systematics of galaxy samples at different redshifts, we carefully construct large and homogeneous galaxy samples with similar stellar mass distributions. We stack the galaxy spectra in our samples, and perform the multi-component fitting of model absorption lines and stellar continua to the stacked spectra. We obtain the central (v_{out}) and maximum (v_{max}) outflow velocities, and estimate the mass loading factors (η) that are defined by the ratio of the mass outflow rate to the star formation rate (SFR). Because our optical spectra do not cover all of the absorption lines at each redshift, for investigating the redshift evolution, we compare outflow velocities at different redshifts with the absorption lines whose depths and ionization energies are similar. Na I D and Mg I at $z \sim 0$ –1 (IE ~ 5 –8 eV) and Mg II and C II at $z \sim 1$ –2 (IE ~ 20 eV). We identify, for the first time, that the average value of v_{out} (v_{max}) monotonically increases by 0.1–0.4 dex from $z \sim 0$ to 1 at the 3.0σ (4.9σ) significance levels and $z \sim 1$ to 2 at the 13.4σ (6.4σ) significance levels at a given SFR. Moreover, based on the absorption lines of Na I D at $z \sim 0$, Mg I at $z \sim 1$, and C II at $z \sim 2$, we find that the value of η increases from $z \sim 0$ to 2 by $\eta \propto (1+z)^{1.8 \pm 0.5}$ at a given halo circular velocity v_{cir} , albeit with a potential systematics caused by model parameter choices. The redshift evolution of v_{out} (v_{max}) and η are probably explained by high gas fractions in high-redshift massive galaxies, which is supported by recent radio observations. We obtain a scaling relation of $\eta \propto v_{\text{cir}}^a$ for $a = -0.5 \pm 1.1$ in our $z \sim 0$ galaxies. This scaling relation agrees well with the momentum-driven outflow model ($a = -1$) within the uncertainty.

Keywords: galaxies: formation — galaxies: evolution — galaxies: ISM — galaxies: kinematics and dynamics

1. INTRODUCTION

The large scale structure of the universe is well explained by gravitational interactions based on the Lambda cold dark matter (Λ CDM) model (e.g., [Springel et al. 2005](#)). However, we need additional models to explain small scale structures like galaxies, because these small scales are significantly affected by the baryon physics, such as gas cooling, radiation heating, star formation, and supernovae (SNe). In fact, there is a notable discrepancy between the shapes of the halo mass function predicted by numerical simulations of Λ CDM model and the galaxy stellar mass function confirmed by observations (e.g., [Somerville & Davé 2015](#)). Theoretical studies suggest that this problem of the discrepancy is resolved by the feedback processes that regulate the star formation. Understanding the feedback processes is key to galaxy formation and evolution.

Galactic outflows driven by star-forming activities are one of the plausible sources of the feedback processes. The cold gas is accelerated by the starburst or the SNe, and carried even to the outside of the halos. The lack of the cold gas thus quenches the star formation in the galaxies. Although the outflows make an impact on the star formation activity, their physical mechanisms are still poorly known. Theoretical studies propose some physical processes to launch the galactic outflows such as the thermal pressure of the core-

collapse SNe (e.g., [Larson 1974](#); [Chevalier & Clegg 1985](#); [Springel & Hernquist 2003](#)), the radiation pressure of the starburst (e.g., [Murray et al. 2005](#); [Oppenheimer & Davé 2006](#)), and the cosmic ray pressure (e.g., [Ipavich 1975](#); [Breitschwerdt et al. 1991](#); [Wadepuhl & Springel 2011](#)).

Since the outflow scale is very small in cosmological simulations, major numerical simulations carry out the outflows as subgrid physics. (see [Somerville & Davé 2015](#), for a recent review). On the other hand, some recent simulations employ the explicit thermal feedback generated by SNe with no outflows in subgrid physics, and describe the relation between the outflow and galaxy properties ([Schaye et al. 2015](#); [Muratov et al. 2015](#); [Barai et al. 2015](#)). [Muratov et al. \(2015\)](#) and [Barai et al. \(2015\)](#) predict that outflow properties evolve towards high redshift based on their numerical models. [Mitra et al. \(2015\)](#) support the evolution of the outflow properties with their analytic model including empirical relations.

Optical and ultra-violet (UV) observations investigate the galactic outflows with emission lines ([Lehnert & Heckman 1996a,b](#); [Heckman et al. 1990](#); [Martin 1998](#)), and absorption lines ([Heckman et al. 2000](#); [Schwartz & Martin 2004](#); [Martin 2005](#); [Rupke et al. 2005a,b](#); [Tremonti et al. 2007](#); [Martin & Bouché 2009](#); [Grimes et al. 2009](#); [Alexandroff et al. 2015](#)) that are found in the spectra of outflow galaxies. Particularly, the absorption lines are used to probe outflow velocities of star-forming galaxies at $z \sim 0$ ([Chen et al. 2010](#); [Chisholm](#)

et al. 2015, 2016), at $z \sim 1$ (Sato et al. 2009; Weiner et al. 2009; Martin et al. 2012; Kornei et al. 2012; Rubin et al. 2014; Du et al. 2016), and at $z > 2$ (Shapley et al. 2003; Steidel et al. 2010; Erb et al. 2012; Law et al. 2012; Jones et al. 2013; Shibuya et al. 2014). Moreover, absorption lines of background quasars are used to study the galactic outflows of foreground galaxies on the sight lines of the background quasars (Bouché et al. 2012; Kacprzak et al. 2014; Muzahid et al. 2015; Schroetter et al. 2015, 2016).

Despite many observations in a wide redshift range, it is challenging to study evolution of outflow velocities because of possible systematic errors included in different redshift samples. The literature uses various procedures to measure outflow velocities, such as non-parametric (Weiner et al. 2009; Heckman et al. 2015), one-component (Steidel et al. 2010; Kornei et al. 2012; Shibuya et al. 2014; Du et al. 2016), and two-component methods (Martin 2005; Chen et al. 2010; Martin et al. 2012; Rubin et al. 2014). Moreover, we should compare the samples of galaxies in the same stellar mass and star formation rate (SFR) ranges because the outflow properties depend on the stellar mass and SFR (i.e., Weiner et al. 2009; Erb et al. 2012; Heckman et al. 2015). Although Du et al. (2016) compare outflow velocities of star-forming galaxies at $z \sim 1$ with those at $z \sim 3$ that are derived with the same procedure, Du et al. (2016) cannot make similar galaxy samples at $z \sim 1$ and $z \sim 3$ due to the lack of stellar mass measurements.

In this paper, we investigate the redshift evolution of galactic outflows found in the star-forming galaxies. We use spectra of galaxies at $z \sim 0, 1$, and 2 drawn from the Sloan Digital Sky Survey (SDSS; York et al. 2000), the Deep Evolutionary Exploratory Probe 2 (DEEP2) Galaxy Redshift Survey (Davis et al. 2003, 2007; Newman et al. 2013), and Erb et al. (2006a,b), respectively. The combination of these data sets enables us to study the redshift evolution of outflow velocities based on the samples of star-forming galaxies with the same stellar mass and SFR ranges. Section 2 presents three samples of star-forming galaxies and our methods for spectrum stacking. We explain our analysis to estimate properties of outflowing gas in Section 3. We provide our results of the outflow velocities in Section 4, and discuss the redshift evolution of the outflow properties in Section 5. Section 6 summarizes our results. We calculate stellar masses and SFRs by assuming a Chabrier (2003) initial mass function (IMF). We adopt a Λ CDM cosmology with $\Omega_M = 0.27$, $\Omega_\Lambda = 0.73$, $h = H_0/(100 \text{ km s}^{-1} \text{ Mpc}^{-1}) = 0.70$, $n_s = 0.95$, and $\sigma_8 = 0.82$ throughout this paper, which are the parameters same as those used in Behroozi et al. (2013). All transitions are referred to by their wavelengths in vacuum. Magnitudes are in the AB system.

2. DATA & SAMPLE SELECTION

To study galactic outflows, we construct three samples at $z \sim 0-2$. A $z \sim 0$ sample is drawn from the SDSS Data Release 7 (DR7; Abazajian et al. 2009), a $z \sim 1$ sample is drawn from the DEEP2 Data Release 4 (DR4; Newman et al. 2013), and a $z \sim 2$ sample is drawn from Erb et al. (2006a). Each spectrum of galaxies in three samples does not have the signal-to-noise ratio (S/N) high enough for analysis of absorption lines. We therefore produce high S/N composites by stacking the spectra. In this section, we describe each sample and explain the method of the spectrum stacking. Properties of the stacked spectra are listed in Table 1. We discuss the selection biases

between three samples in Section 4.2.

2.1. Galaxies at $z \sim 0$

We select star-forming galaxies at $z \sim 0$ from the SDSS DR7 (Abazajian et al. 2009) main galaxy sample (Strauss et al. 2002). The spectra of these galaxies have a mean spectral resolution of $R \sim 2000$, a dispersion of $69 \text{ km s}^{-1} \text{ pixel}^{-1}$, and a wavelength coverage spanning between 3800 and 9200 Å. These spectra are taken with fibers of a $3''$ diameter, that are placed at the center of the galaxies. The SDSS imaging data are taken through a set of u, g, r, i , and z filters (Fukugita et al. 1996) using a drift-scanning mosaic CCD camera (Gunn et al. 1998).

Since our targets are active star-forming disk galaxies, we need some galaxy properties for sample selection. The galaxy properties are mainly taken from the MPA/JHU galaxy catalog¹. Systemic redshifts z_{sys} are derived with observed spectra and a linear combination of the galaxy template spectra. Because this measurement may be affected by blueshifted absorption that outflowing gas produce, we compare z_{sys} in the MPA/JHU catalog with redshifts measured by fitting H α emission lines alone with a Gaussian function. We find that the difference of the two redshifts is typically $< 5 \text{ km s}^{-1}$ and negligible. Stellar masses M_* are obtained by the fitting to the photometry (Kauffmann et al. 2003; Salim et al. 2007). SFRs within the fiber (SFR_{fiber}) are measured from the extinction-corrected H α emission-line flux, and total SFR are estimated by applying aperture correction with the photometry outside the fiber (Brinchmann et al. 2004). For our study, stellar masses and SFRs are converted from a Kroupa (2001) IMF to a Chabrier (2003) IMF with a correction factor of 0.93. SFR surface densities Σ_{SFR} are defined as $\text{SFR}_{\text{fiber}}/\pi R^2$, where R is the physical length corresponding to the SDSS $1.5''$ aperture radius. The MPA/JHU catalog also includes the emission- and absorption-line fluxes (e.g., H α , H β , [O III], [N II] and $D_n(4000)$; Tremonti et al. 2004) and the photometric properties (e.g., five photometric magnitudes). As a parameter to distinguish disk galaxies from ellipticals, we use the fracDeV (Abazajian et al. 2004), which is the coefficient of the best linear fitting that is a combination of exponential and de Vaucouleurs (1948) rules. When the fracDeVs of galaxies are less/greater than 0.8, they are defined as disk/elliptical galaxies. Because our targets are disk galaxies, we use the axial ratio of the exponential fitting. Using Table 8 in Padilla & Strauss (2008), we calculate the inclinations, i , of our galaxies from the r -band axial ratios and absolute magnitudes.

We use the similar criteria used by Chen et al. (2010) to select the star-forming galaxies from the main galaxy sample (Strauss et al. 2002), which contains the galaxies with extinction-corrected Petrosian r magnitude in the range of $14.5 < r < 17.5$. The values of z_{sys} range from 0.05 to 0.18. To select active star-forming disk galaxies, we apply the criteria of $D_n(4000)$ less than 1.5 and r -band fracDeV less than 0.8. Active galactic nuclei (AGN) are excluded with the classification by Kauffmann et al. (2003). We also exclude the galaxies whose SFRs or stellar masses are not derived in the MPA/JHU catalog. Moreover, we set two additional selection criteria for our study. First, we select the galaxies with $\Sigma_{\text{SFR}} \geq 10^{-0.8} \text{ M}_\odot \text{ yr}^{-1} \text{ kpc}^{-2}$, which is above the empirical threshold $\Sigma_{\text{SFR}} > 0.1 \text{ M}_\odot \text{ yr}^{-1} \text{ kpc}^{-2}$ for local galaxies

¹ The MPA/JHU galaxy catalog is available at <http://www.mpa-garching.mpg.de/SDSS/DR7>

Table 1
Properties of the stacked spectra

sample	line	number ^a	z^b	SFR ^c ($M_\odot \text{ yr}^{-1}$)	M_*^d (M_\odot)	v_{out}^e (km s^{-1})	v_{max}^f (km s^{-1})	η^g
z0-sample	Na I D	125	0.063	0.44	10.1	144 ± 6	211 ± 21	2.1 ± 1.7
	Na I D	114	0.072	0.62	10.2	130 ± 5	218 ± 15	1.7 ± 1.0
	Na I D	118	0.079	0.74	10.3	138 ± 5	269 ± 12	2.1 ± 0.92
	Na I D	123	0.098	0.86	10.4	151 ± 15	301 ± 30	1.9 ± 1.1
	Na I D	133	0.12	1.0	10.5	146 ± 15	308 ± 31	1.7 ± 0.99
	Na I D	172	0.16	1.3	10.8	162 ± 15	353 ± 27	1.5 ± 0.79
z1-sample	Mg I	665	1.4	0.70	9.96	228 ± 35	504 ± 60	11 ± 7.5
	Mg I	395	1.4	0.92	10.3	166 ± 16	315 ± 69	2.5 ± 3.5
	Mg I	277	1.4	1.2	10.6	171 ± 20	395 ± 99	2.8 ± 4.4
	Mg II	665	1.4	0.70	9.96	161 ± 8	431 ± 20	3.9 ± 2.4
	Mg II	395	1.4	0.92	10.3	148 ± 9	452 ± 25	3.7 ± 2.5
	Mg II	277	1.4	1.2	10.6	203 ± 6	576 ± 21	3.5 ± 2.0
z2-sample	C II	25	2.2	1.4	10.3	439 ± 25	865 ± 25	15 ± 5.6
	C IV	25	2.2	1.4	10.3	429 ± 17	855 ± 17	19 ± 6.2

^a Number of galaxies used for a composite spectrum.

^b Median redshift

^c Median star formation rate

^d Median stellar mass

^e Central outflow velocity defined in Section 4.1

^f Maximum outflow velocity defined in Section 4.1

^g Mass loading factor defined in Section 5.1

to launch outflows (Heckman 2002). Second, we chose face-on galaxies whose inclinations are $i < 40^\circ$ because the typical opening angle of the outflows is $< 60^\circ$ for the SDSS galaxies (Chen et al. 2010). There are 2734 galaxies that satisfy all of the selection criteria. The blue dashed line in Figure 1 indicate the normalized distribution of stellar masses for this sample. In order to make samples with similar stellar mass distribution at $z \sim 0-2$, we randomly select the high-mass galaxies from the sample to match the distribution of the sample at $z \sim 0$ to that of the sample at $z \sim 1$ (Section 2.2). The final galaxy sample contains 785 galaxies. We refer to the final sample as the z0-sample. The normalized distribution of stellar masses for the z0-sample is shown in Figure 1 with the blue solid line. The median stellar mass of the z0-sample is $\log(M_*/M_\odot) = 10.37$.

We produce high S/N composites by stacking the spectra. Regarding each individual spectrum, the wavelength is shifted to the rest-frame with z_{sys} , and the flux is normalized to the continuum around Na I D $\lambda\lambda 5891.58, 5897.56$. Since bad pixels are identified as OR_MASK by the SDSS reduction pipeline, we exclude them in the same manner as Chen et al. (2010). These individual spectra are combined with an inverse-variance weighted mean. We divide the z0-sample into SFR bins where the composite spectra have S/N per pixel of 300 in the range of 6000–6050 Å.

2.2. Galaxies at $z \sim 1$

For our galaxies at $z \sim 1$, we use the DEEP2 DR4 (Newman et al. 2013)². The survey is conducted with the DEIMOS (Faber et al. 2003) at the Keck II telescope. The DEEP2 survey targets galaxies with a magnitude limit of $18.5 < R_{\text{AB}} < 24.1$ in four fields of the Northern Sky. In three of the four fields, the DEEP2 survey preselect these galaxies with B , R , and I photometry taken with 12K camera at the Canada-France-Hawaii Telescope to remove galaxies at $z < 0.7$ (Coil et al. 2004). The spectra of these galaxies are taken with a 1200 lines/mm grating and a $1''0$ slit. The spectral setting gives $R \sim 5000$. The wavelength ranges from 6500 to 9100 Å.

The public data are reduced with the DEEP2 DEIMOS Data pipeline (the *spec2d* pipeline; Newman et al. 2013; Cooper et al. 2012). In addition we execute IDL routines for the flux calibration of the DEEP2 spectra (Newman et al. 2013). The IDL routines correct spectra for the overall throughput, chip-to-chip variations, and telluric contamination. After these corrections, the IDL routines calibrate fluxes of the spectra with the R - and I -band photometry. The flux calibration is accurate to 10% or better. Since the routines can not calibrate some spectra correctly, we exclude the spectra from our sample.

We use galaxy properties taken from the DEEP2 DR4 redshift catalog. The catalog includes the absolute B -band magnitude M_B , $(U-B)$ color in the rest frame, systemic redshift z_{sys} , and object classification. The last two parameters are determined by the *spec1d* redshift pipeline. The *spec1d* pipeline finds the best value of z_{sys} with galaxy-, QSO-, and star-template spectra to minimize χ^2 of the data and the templates (Newman et al. 2013). The error of z_{sys} is $\sim 16 \text{ km s}^{-1}$. We also use $(B-V)$ color measured by C. N. A. Willmer (in private communication).

Since we need the spectra within which Mg II $\lambda\lambda 2796, 2803$ absorption lines fall, we firstly adopt the criteria used in Weiner et al. (2009). Weiner et al. (2009) select the spectra extending to 2788.7 Å in the rest frame. To avoid the AGN/QSO contamination, Weiner et al. (2009) exclude the galaxies at $z \geq 1.5$ or having the AGN classification of Newman et al. (2013). In addition to these criteria of Weiner et al. (2009), we remove galaxies that are at the red sequence (Willmer et al. 2006; Martin et al. 2012). We also remove the low-S/N galaxies that significantly affect the normalization procedure described below. Our final sample contains 1337 galaxies at $1.2 \lesssim z_{\text{sys}} < 1.5$ with the median value $\langle z \rangle = 1.37$. We refer to this sample as the z1-sample. The normalized distribution of stellar masses for the z1-sample is shown in Figure 1 with the green line. The median stellar mass of the z1-sample is $\log(M_*/M_\odot) = 10.24$.

We estimate stellar masses and SFRs from equations in the literature. Stellar masses are calculated from M_B , $(U-B)$, and $(B-V)$ colors by Equation (1) of Lin et al. (2007). We rewrite

² The DEEP2 DR4 is available at <http://deep.ps.uci.edu/DR4/home.html>

the equation from Vega to AB magnitudes using the transformation in Willmer et al. (2006) and Blanton & Roweis (2007):

$$\begin{aligned} \log(M_*/M_\odot) = & -0.4(M_B - 5.48) + 1.737(B - V) \\ & + 0.309(U - B) - 0.130(U - B)^2 \\ & - 0.268z + 1.123. \end{aligned} \quad (1)$$

SFRs are also calculated from M_B and $(U - B)$. Using Equation (1) and Table 3 of Mostek et al. (2012), we derive SFRs by

$$\text{SFR} = 0.381 - 0.424M_B - 2.925(U - B) - 2.603(U - B)^2. \quad (2)$$

The quantities of the SFRs are calculated with a Salpeter (1955) IMF. To obtain the quantities in a Chabrier (2003) IMF, we apply a correction factor of 0.62.

Stacked spectra are produced in the same manner as in Section 2.1, but with three procedures for the $z1$ -sample. The first procedure is to convert wavelength from air to vacuum by the method of Ciddor (1996). The second one is to normalize the flux at the continuum measured in the wavelength range around Mg II $\lambda\lambda 2796.35, 2803.53$. The third one is to divide the $z1$ -sample into three subsamples in low, medium, and high SFR bins.

2.3. Galaxies at $z \sim 2$

We use the sample of Erb et al. (2006a) for our sample at $z \sim 2$. The sample consists of BX/BM (Adelberger et al. 2004; Steidel et al. 2004) and MD (Steidel et al. 2003) galaxies, which are originally in the rest-frame UV-selected sample described by Steidel et al. (2004). The rest-frame UV spectra of galaxies are taken with the LRIS at the Keck I telescope, and the near-infrared (NIR) spectra are mainly taken with NIRSPEC (McLean et al. 1998) at Keck II telescope. Since our aim is to analyze rest-frame UV absorption lines, we obtain the raw data taken with the 400/3400 grism of LRIS-B from 2002 to 2003 (PI Steidel) through the Keck Observatory Archive³ (KOA). The spectral resolution is $R \sim 800$. The wavelength ranges from 3000 to 5500 Å.

The data are reduced with the XIDL LowRedux⁴ pipeline. Right ascension (R.A.) and declination (Decl.) of each galaxy are derived from the pixel values and the fits header of data with the program COORDINATES⁵. We find systematic errors of about $20''$ in results of COORDINATES. However, since some galaxies are observed with one mask at the same time, we can correct R.A. and Decl. of them to be consistent with coordinates of Erb et al. (2006a). As shown in Steidel et al. (2010), this sample contains galaxy–galaxy pairs; the circumgalactic medium around foreground galaxies give rise to absorption lines in the spectra of the background galaxies. For this reason, we remove 6 background galaxies of the galaxy–galaxy pairs from our sample. Finally, we obtain the spectra of 25 galaxies in the Erb et al. (2006a) sample. We refer to this sample as the $z2$ -sample. The normalized distribution of stellar masses for the $z2$ -sample is shown in Figure 1 with the orange line. The median stellar mass of the $z2$ -sample is $\log(M_*/M_\odot) = 10.28$.

We take z_{sys} , stellar masses, and SFRs of the $z2$ -sample from Erb et al. (2006a). The systemic redshifts z_{sys} are de-

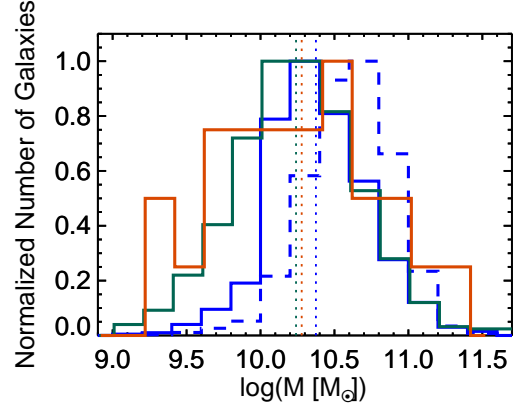


Figure 1. Normalized histograms of the stellar masses for the three samples. The blue, green, and orange solid lines indicate 785 galaxies in the $z0$ -sample, 1337 galaxies in the $z1$ -sample, and 25 galaxies in the $z2$ -sample, respectively. The blue dashed line denotes the SDSS galaxies that satisfy the selection criteria. The blue, green, and orange vertical dotted lines show the median stellar masses of the $z0$ -, $z1$ -, and $z2$ -samples. Each histogram is normalized to the maximum number of the bins.

termined by the $H\alpha$ emission line on the NIR spectra. The typical rms error of z_{sys} is 60 km s^{-1} (Steidel et al. 2010). Stellar masses and SFRs are derived from the SED fitting with the U_n , G , R , J , and K -band magnitudes. The mid-infrared magnitudes taken with Infrared Array Camera on the Spitzer Space Telescope are also used, if they are available.

Stacked spectra are produced in the same manner as in Section 2.1, but with four procedures for the $z2$ -sample: (1) to convert the wavelength from air to vacuum; (2) to normalize the flux in the wavelength range between 1410 and 1460 Å; (3) not to exclude bad pixels since they are not detected by the pipeline; and (4) not to divide the $z2$ -sample into subsamples.

3. ANALYSIS

We analyze metal absorption lines in the galaxy spectra to study the outflow properties. The absorption lines are Na I D $\lambda\lambda 5891.58, 5897.56$ for $z0$ -sample; Mg I $\lambda 2852.96$ and Mg II $\lambda\lambda 2796.35, 2803.53$ for $z1$ -sample; and C II $\lambda 1334.53$, and C IV $\lambda\lambda 1548.20, 1550.78$ for $z2$ -sample. We assume that absorption profiles consist of three components: the intrinsic component composed of the stellar absorption and the nebular emission lines, the systemic component produced by the static gas in the interstellar medium (ISM) of the galaxies, and the outflow component produced by the outflowing gas from the galaxies. The stellar atmospheres of cool stars specifically give rise to the strong Na I D absorption, which impacts on the results of the outflow analysis (Chen et al. 2010). The stellar atmospheres also provide moderate absorption features of Mg I, Mg II, C II and C IV (Rubin et al. 2010; Coil et al. 2011; Steidel et al. 2016). Additionally, the static gas in the ISM produces absorption lines at the systemic velocity while the outflowing gas makes blueshifted absorption lines. (e.g., Martin 2005; Chen et al. 2010; Rubin et al. 2014). We follow the procedures of the analysis shown in Chen et al. (2010). Below, we explain the procedures that are made in two steps. First, we determine the stellar continuum of the stacked spectra for the intrinsic components of the absorption lines. Second, we model the absorption lines with the stellar continuum and obtain the outflow components.

3.1. Stellar Continuum Determination

³ KOA website: <http://www2.keck.hawaii.edu/koa/public/koa.php>

⁴ The XIDL LowRedux is available at <http://www.ucolick.org/~xavir/LowRedux/>

⁵ COORDINATES is available at <http://www2.keck.hawaii.edu/inst/lris/coordinates.html>

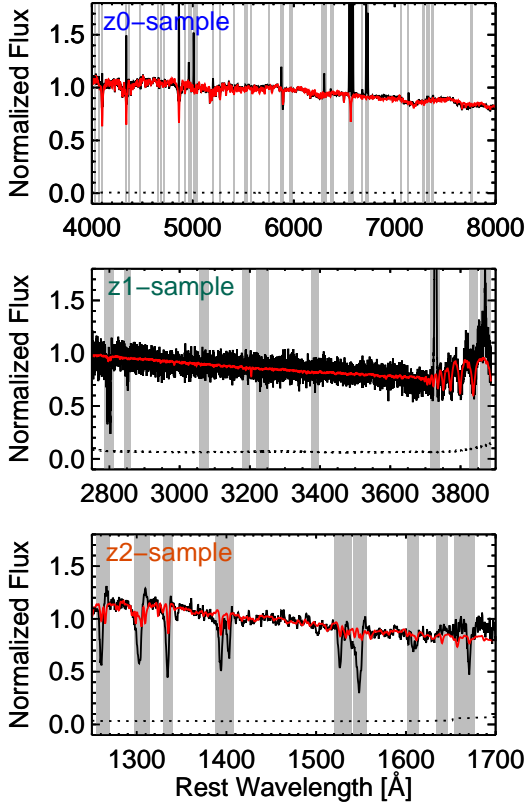


Figure 2. Examples of the stacked spectra (black line) and the best-fitting continuum models (red line). The spectra of the z_0 -, z_1 -, and z_2 -samples are shown from top to bottom. The wavelength range shown in this figure is used for the stellar continuum fitting, except for the gray shading. The dotted lines denote 1σ uncertainties of the spectra.

We determine the stellar continuum with simple stellar population (SSP) models. For the z_0 -sample, we adopt [Bruzual & Charlot \(2003\)](#) SSP models, which have a high spectral resolution in the wavelength of the SDSS spectra. We use the 30 template spectra with 10 ages of 0.005, 0.025, 0.1, 0.29, 0.64, 0.90, 1.4, 2.5, 5, and 11 Gyr, and three metallicities of $Z = 0.004, 0.02$, and 0.05 . On the other hand, for the z_1 - and z_2 -samples, we adopt [Maraston et al. \(2009\)](#) SSP models based on Salpeter IMF because the template spectra of [Bruzual & Charlot \(2003\)](#) models have a low spectral resolution at wavelengths less than 3300 \AA . [Maraston et al. \(2009\)](#) models have a high spectral resolution of $R \sim 10000$ in the wavelength range of $1000-4700 \text{ \AA}$. We use the 30 template spectra with 10 ages of 1, 5, 25, 50, 100, 200, 300, 400, 650, and 900 Myr, and three metallicities of $Z = 0.001, 0.01$, and 0.02 . For all samples, each template spectrum is convolved with the stellar velocity dispersion of each stacked spectrum. We construct the best fitting models of the stacked spectra with a linear combination of the template spectra applying the starburst extinction curve of [Calzetti et al. \(2000\)](#) by the IDL routine MPFIT ([Markwardt 2009](#)). We make the linear combination of all 30 template spectra and fit to the z_0 -sample composite spectra, which have high S/N. We perform the same analysis of the z_1 - and z_2 -sample spectra, but with the linear combination of 10 template spectra of a fixed metallicity. Since our main results are insensitive to differences of metallicity, we use $Z = 0.01$ for z_1 - and z_2 -samples. The rest-

frame wavelength ranges used for fitting are $4000-7000 \text{ \AA}$ for the z_0 -sample, $2750-3500 \text{ \AA}$ for the z_1 -sample, and $1200-1600 \text{ \AA}$ for the z_2 -sample. In the fitting we omit the wavelength ranges of all of the emission and absorption lines except for made by the stellar atmosphere. Figure 2 shows the stacked spectra (black) and the best fitting models (red) of the z_0 -, z_1 -, and z_2 -samples.

3.2. Outflow Profile Estimate

With the best fitting models of the stellar continuum, we estimate the systemic and outflow components of the absorption lines. The normalized absorption profile $I_{\text{obs}}(\lambda)$ is assumed to be expressed by three components:

$$I_{\text{obs}}(\lambda) = I_{\text{int}}(\lambda) I_{\text{sys}}(\lambda) I_{\text{out}}(\lambda), \quad (3)$$

where $I_{\text{int}}(\lambda)$, $I_{\text{sys}}(\lambda)$ and $I_{\text{out}}(\lambda)$ are the intrinsic, systemic, and outflow components, respectively. We use the stellar continuum given in Section 3.1 for $I_{\text{int}}(\lambda)$, except for Na I D and Mg II cases that are explained later in (ii) and (iii), respectively. We adopt a model made from a set of following two equations for each of the systemic and outflow components ([Rupke et al. 2005a](#)). In this model, the normalized line intensity $I(\lambda)$ is given by

$$I(\lambda) = 1 - C_f + C_f e^{-\tau(\lambda)}, \quad (4)$$

where $\tau(\lambda)$ is the optical depth, and C_f is the covering factor. Although C_f may be a function of wavelength ([Martin & Bouché 2009](#)), we assume that C_f is independent of wavelength. Under the curve-of-growth assumption, the optical depth is written with a Gaussian function as

$$\tau(\lambda) = \tau_0 e^{-(\lambda - \lambda_0)^2 / (\lambda_0 b_D / c)^2}. \quad (5)$$

where c is the speed of light, τ_0 is the optical depth at the central wavelength λ_0 of the line, and b_D is the Doppler parameter in units of speed. There are 4 parameters for each of $I_{\text{out}}(\lambda)$ (i.e., $\lambda_{0,\text{out}}$, $\tau_{0,\text{out}}$, $C_{f,\text{out}}$, and $b_{D,\text{out}}$) and $I_{\text{sys}}(\lambda)$ (i.e., $\lambda_{0,\text{sys}}$, $\tau_{0,\text{sys}}$, $C_{f,\text{sys}}$, and $b_{D,\text{sys}}$). Because the central wavelength $\lambda_{0,\text{sys}}$ of $I_{\text{sys}}(\lambda)$ is fixed to the rest-frame wavelength λ_{rest} . Hence, the model of $I_{\text{obs}}(\lambda)$ includes 7 ($= 4 + 3$) free parameters in total.

Equation (3) is modified in the following three cases. (i) The first case is applied for the doublet lines (Na I D, Mg II, and C IV). We define the optical depth of the blue and red lines of the doublet as $\tau_B(\lambda)$ and $\tau_R(\lambda)$ whose central wavelengths are $\lambda_{0,B}$ and $\lambda_{0,R}$, respectively. The total optical depth is written as $\tau(\lambda) = \tau_B(\lambda) + \tau_R(\lambda)$. Because the blue lines have oscillator strengths twice higher than the red lines for all of the doublet lines, the central optical depths of the blue lines $\tau_{0,B}$ are related to those of the red lines $\tau_{0,R}$ by $\tau_{0,R} = \tau_{0,B}/2$. The ratio of the central wavelengths $\lambda_{0,B}/\lambda_{0,R}$ of the outflow component is fixed to the rest-frame doublet wavelengths ratio. We assume that b_D and C_f for the blue and red lines are the same since these lines should arise from the same gas clumps. The number of free parameters therefore remains unchanged. (ii) The second case is applied for Na I D, which has a neighboring emission line He I $\lambda 5877.29$. We model the emission line profile $I_{\text{emi}}(\lambda)$ of He I using a Gaussian function with additional 2 free parameters. In this case, the intrinsic component of Equation (3) is expressed as

$$I_{\text{int}}(\lambda) = I_{\text{cont}}(\lambda) + I_{\text{emi}}(\lambda), \quad (6)$$

where $I_{\text{cont}}(\lambda)$ is the stellar continuum given in Section 3.1. For Na I D, there are the total of 9 ($= 7 + 2$) free parameters in

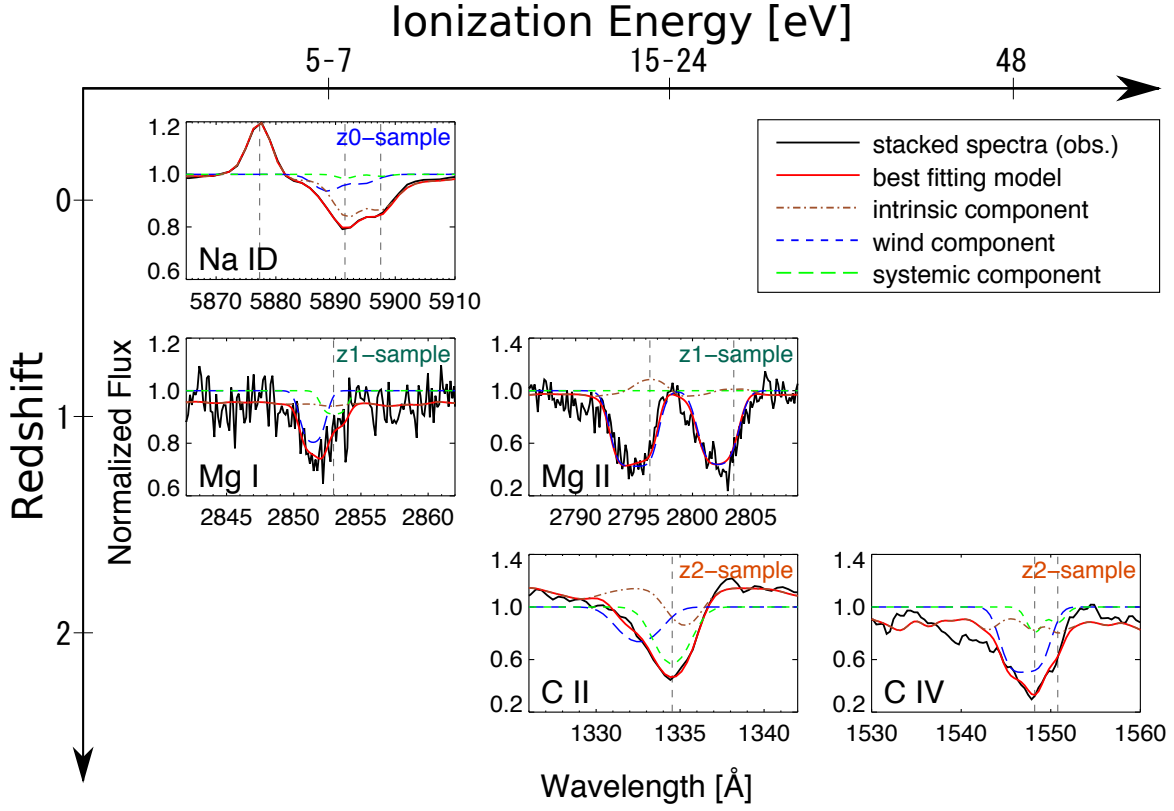


Figure 3. Examples of the stacked spectra around the absorption lines (black line). The red lines represent the best fitting models. The dot-dashed brown, dashed blue, and long-dashed green indicate the breakdowns of the lines for the intrinsic, wind, and systemic components, respectively. In this figure, the redshift (the ionization energy) increase from top to bottom (from left to right). The ions of the absorption lines are written at the bottom-left corner of the panels, and the samples are written at the top-right corner. The vertical dashed gray lines denote the rest-frame wavelengths of the absorption lines, except for the line at 5877.29 Å in the top-left panel, which represents the wavelengths of He I emission.

$I_{\text{obs}}(\lambda)$ that are composed of 7 free parameters of Equations (4)–(5) and the 2 parameters of the Gaussian function $I_{\text{emi}}(\lambda)$. (iii) The third case is applied for Mg II. We identify P-Cygni profiles of Mg II absorption lines in the stacked spectra, which are found by previous studies (e.g., Weiner et al. 2009; Rubin et al. 2011; Erb et al. 2012; Martin et al. 2013). The emission component of the P-Cygni profile prevent us from modeling the systemic components $I_{\text{sys}}(\lambda)$ as absorption lines. We assume that the center of $I_{\text{emi}}(\lambda)$ is fixed to the rest-frame wavelength λ_{rest} of Mg II, and that $I_{\text{sys}}(\lambda)$ is unity to avoid degeneracy between the emission $I_{\text{emi}}(\lambda)$ and the absorption $I_{\text{sys}}(\lambda)$. $I_{\text{int}}(\lambda)$ of Equation (3) is given by Equation (6).

We carry out the model fitting and obtain the best fit of each absorption line with MPFIT. Since Martin & Bouché (2009) show that covering factors of Na I D and Mg I are smaller than those of Mg II, we limit the range of $C_{f,\text{out}}$ to $0 \leq C_{f,\text{out}} \leq 0.2$ ($0 \leq C_{f,\text{out}} \leq 1$) for Na I D and Mg I (the other absorption lines). Figure 3 shows the examples of the fitting results. Our procedure provides the reasonable results, and detect the blueshifted outflow components that are shown with the dashed blue lines in Figure 3. We note that there exists a plausible shallow absorption around 1540 Å in the bottom-right panel of Figure 3. This shallow absorption may arise from stellar winds of young stars that broaden the C IV absorption line (Schwartz & Martin 2004; Schwartz et al. 2006). Although the outflow components are determined by a deep C IV absorption line, the shallow absorption may produce a systematic uncertainty of the outflow velocities. Du et al. (2016) reproduce the shallow absorption with SSP

model from Leitherer et al. (2010) that includes the predicted effects of the stellar wind. Because we do not use the C IV absorption line for discussion, the results of C IV are not relevant to our main scientific results.

4. RESULTS

4.1. Outflow Velocity

We define the velocity of the outflowing gas in two ways: the central outflow velocity $v_{\text{out}} = c(\lambda_{\text{sys}} - \lambda_{0,\text{out}})/\lambda_{\text{sys}}$ and the maximum outflow velocity $v_{\text{max}} = c(\lambda_{\text{sys}} - \lambda_{\text{max}})/\lambda_{\text{sys}}$. The maximum wavelength λ_{max} is defined as

$$\lambda_{\text{max}} = \lambda_{0,\text{out}} - \lambda_{0,\text{out}} \frac{b_{D,\text{out}}}{c} \sqrt{-\ln \left(\frac{1}{\tau_{0,\text{out}}} \ln \frac{1}{0.9} \right)}, \quad (7)$$

at which the blue side of the outflow component reaches 90 % of the flux from $1 - C_f$ to unity, i.e., $I_{\text{out}}(\lambda_{\text{max}}) = 0.9(1 - C_f)$. The central outflow velocity v_{out} is the central velocity of the outflowing gas, which represents the bulk motion of the gas. In contrast, the maximum outflow velocity v_{max} reflects the gas motion at the largest radii of the outflows, based on the simple scenario that the outflowing gas is accelerated towards the outside of the halo (Martin & Bouché 2009). Therefore, v_{max} is the indicator of whether the outflowing gas can escape the galactic halo to the inter-galactic medium (IGM).

Figures 4–6 show v_{out} and v_{max} as a function of SFRs. In Figure 4, v_{out} and v_{max} of the z0-sample (shown with the blue circles) are as high as those of galaxies at $z \sim 0$ in the literature (shown with the open symbols). We perform a power-

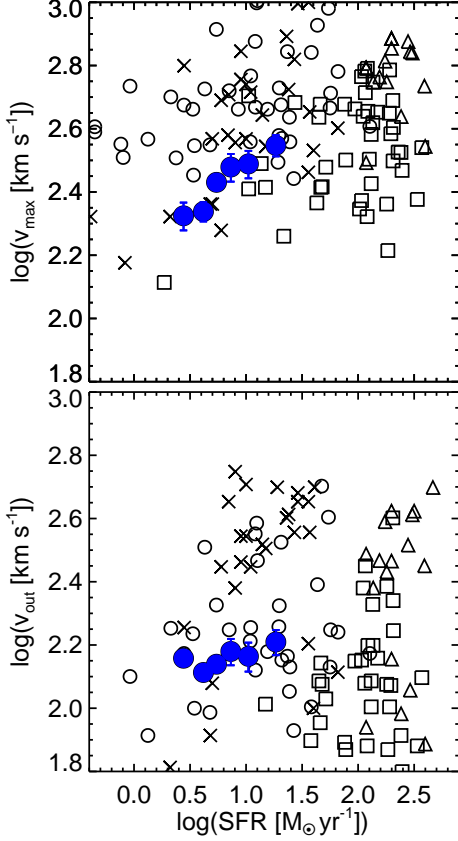


Figure 4. The outflow velocities at $z \sim 0$. Top: the maximum outflow velocities (blue filled circle) of the $z0$ -sample as a function of SFRs. Error bars denote the 1σ fitting error. The open symbols show the maximum outflow velocities of local galaxies in the literature: Heckman et al. (2015, cross), Martin (2005, triangle), Rupke et al. (2005b, square), and Chisholm et al. (2015, circle). Bottom: the central outflow velocities of the $z0$ -sample. The symbols are the same as those in the top panel of this figure.

law fitting to v_{out} and v_{max} with the form of $V = V_1 \text{SFR}^\alpha$. The best-fit parameters are $V_1 = 10^{2.11 \pm 0.03}$ and $\alpha = 0.05 \pm 0.04$ for $V = v_{\text{out}}$; and $V_1 = 10^{2.21 \pm 0.05}$ and $\alpha = 0.28 \pm 0.05$ for $V = v_{\text{max}}$. Using the SDSS DR7 galaxies same as ours, Chen et al. (2010) find a scaling relation of v_{out} flatter than the one of $\alpha = 0.35 \pm 0.06$ found by Martin (2005). Martin et al. (2012) also find no correlation between v_{out} and SFR. Although Chen et al. (2010) and Martin et al. (2012) do not calculate the scaling factor α for v_{out} , the trend of v_{out} is consistent with our results. On the other hand, Martin et al. (2012) show that their results and previous studies of v_{max} are consistent with the scaling factor of $\alpha = 0.35 \pm 0.06$ (Martin 2005). Our measurement of $\alpha = 0.28 \pm 0.05$ for v_{max} agrees with this steep trend.

Figure 5 compares v_{out} and v_{max} of the $z1$ -sample with those of galaxies at $z \sim 1$ in the literature. The $z1$ -sample shown with the green symbols is in good agreement with the literature. Particularly, the values of v_{max} is consistent with those in Weiner et al. (2009), who use the DEEP2 DR3 spectra. We also find the weak positive scaling relation between v_{out} and SFR. In the literature, whereas v_{out} of individual galaxies show no correlation (Kornei et al. 2012; Martin et al. 2012; Rubin et al. 2014), those of stacked galaxies show the positive correlation (Weiner et al. 2009; Bordoloi et al. 2014). The positive scaling relation in Figure 5 (the green symbols)

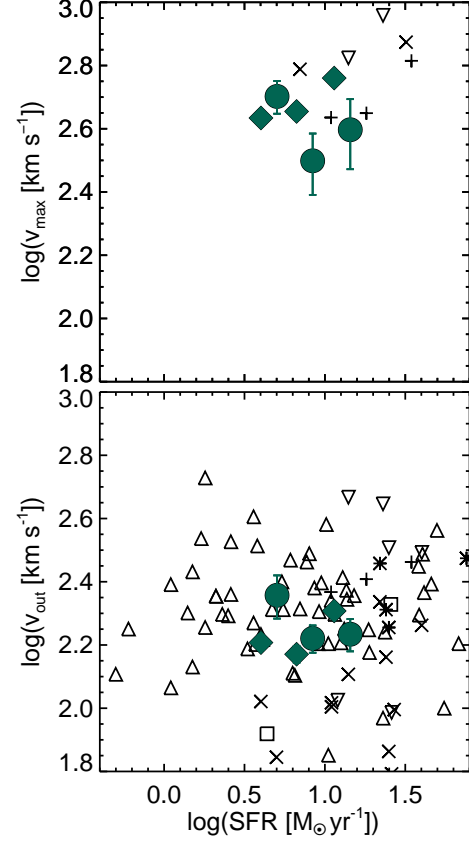


Figure 5. Same as Figure 5, but for the outflow velocities at $z \sim 1$. Top: the maximum outflow velocities of the $z1$ -sample for Mg I and Mg II (green filled circle and diamond, respectively) as a function of SFRs. Error bars denote the 1σ fitting errors. The open symbols show the maximum outflow velocities of galaxies at $z \sim 0.5-1$ in the literature: Kornei et al. (2012, cross), Rubin et al. (2014, triangle), Bordoloi et al. (2014, square), Weiner et al. (2009, plus), Martin et al. (2012, upside-down triangle), and Du et al. (2016, asterisk). Bottom: the central outflow velocities of the $z1$ -sample. The symbols are the same as those in the top panel of this figure. In both panels, the green diamonds are offset in SFR by 0.1 dex for clarity.

are consistent with the previous results of the stacked galaxies.

Figure 6 compares the $z2$ -sample and the literature at $z \sim 2$. Steidel et al. (2010) study the outflow velocities (Δv_{IS}) of the UV-selected galaxies at $z \sim 2$ with the sample drawn from Erb et al. (2006a). The mean outflow velocity ($\langle \Delta v_{\text{IS}} \rangle = -164 \pm 16 \text{ km s}^{-1}$) is lower than v_{out} of the $z2$ -sample (shown with the orange symbols). This arises from different methods to measure the velocities: the outflow velocity become lower with the one-component fitting than with the two-component fitting. Therefore, it is reasonable that Δv_{IS} is lower than v_{out} , even though $z2$ -sample is a subsample drawn from Erb et al. (2006a). Steidel et al. (2010) also find that the scaling relation of central outflow velocities at $z \gtrsim 2$ is flatter than that at $z < 2$, but we can not mention the scaling relation of the $z2$ -sample due to the small sample size.

4.2. Evolution of Outflow Velocity

We show v_{max} measurements of our $z0$ -, $z1$ -, and $z2$ -samples as a function of SFRs with the blue, green, and orange symbols, respectively, in the top panel of Figure 7. The bottom panel is the same as the top panel, but for v_{out} . Figure 7 indicates the increasing trend of the outflow velocity with in-

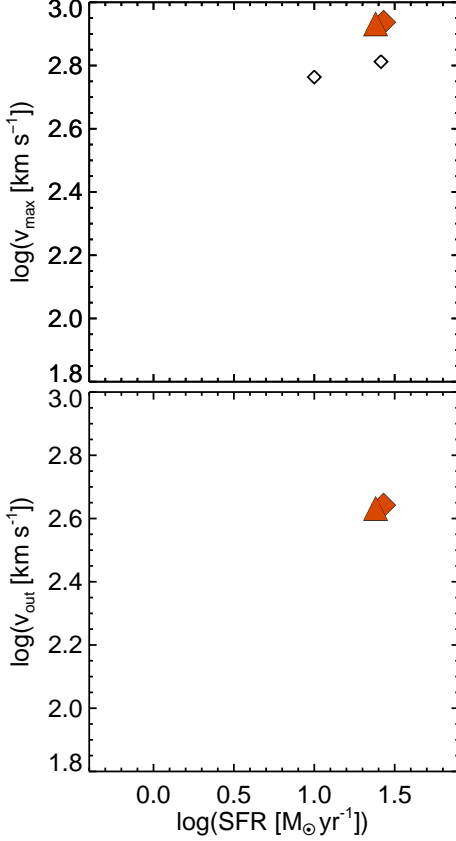


Figure 6. Same as Figure 4, but for the central outflow velocities at $z \sim 2$. The orange diamond and triangle indicate the central outflow velocities of the $z2$ -sample for C II and C IV, respectively. Error bars denote the 1σ fitting errors. The open diamonds show the maximum outflow velocities of galaxies in Erb et al. (2012). The orange triangle is offset in SFR by 0.1 dex for clarity.

creasing redshift. Martin & Bouché (2009) and Chisholm et al. (2016) indicate that the outflow velocity depends on the depths of the absorption lines whereas Tanner et al. (2016) show that the outflow velocity depends on ionization energy (IE) of the ions used for velocity measurements. For these reasons, we compare the outflow velocities of the absorption lines that have the similar depths and IE, which is presented in Figure 3. The details of our comparisons are explained below.

To compare the $z0$ - with $z1$ -samples, we use v_{out} and v_{max} computed from Na I D (IE $\simeq 5.1$ eV) and Mg I (IE $\simeq 7.6$ eV) absorption lines, respectively, which are depicted with the circles in Figure 7. In Section 4.1, we obtain the best-fit parameter sets of the scaling relation $V = V_1 \text{SFR}^\alpha$ for Na I D of the $z0$ -sample: $V_1 = 10^{2.11 \pm 0.03}$ ($10^{2.21 \pm 0.05}$) and $\alpha = 0.05 \pm 0.04$ (0.28 ± 0.05) for $V = v_{\text{out}}$ (v_{max}). We perform a power-law fitting to v_{out} (v_{max}) for Na I D of the $z0$ -sample and Mg I of the $z1$ -sample with the slope fixed at $\alpha = 0.05$ (0.28). The best-fit parameter sets are $V_1 = 10^{2.11 \pm 0.01}$ ($10^{2.21 \pm 0.01}$) and $V_1 = 10^{2.20 \pm 0.03}$ ($10^{2.41 \pm 0.04}$) for Na I D and Mg I, respectively. We find that v_{out} (v_{max}) at $z \sim 1$ is higher than the one at $z \sim 0$ at the 3.0σ (4.9σ) significance level. The blue and green shades in Figure 7 illustrate the best-fitting relations of Na I D at $z \sim 0$ and Mg I at $z \sim 1$, respectively. The widths of the shades represent the 1σ fitting error ranges.

To compare the $z1$ - with $z2$ -samples, we use v_{out} and v_{max} computed from Mg II (IE $\simeq 15$ eV) and C II (IE $\simeq 24$ eV)

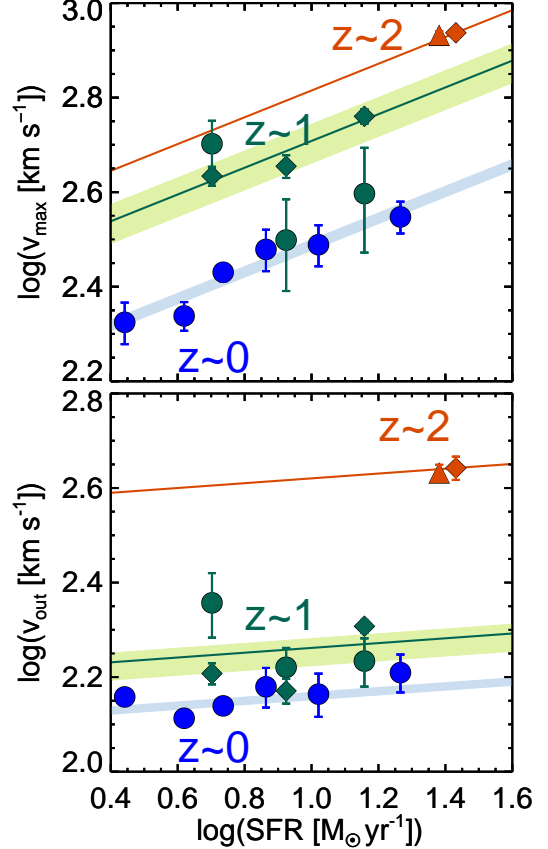


Figure 7. Same as Figure 4, but for the $z0$ - (blue symbol), $z1$ - (green symbol), and $z2$ - (red symbol) samples. Top: the maximum outflow velocities as a function of SFRs. Each symbol corresponds to the elements of the absorption lines: Na I D (blue circle), Mg I (green circle), Mg II (green diamond), C II (orange diamond), and C IV (orange triangle). The circles, diamonds, and triangle indicate the velocities of elements, which have the low (5–7 eV), medium (15–24 eV), and high (48 eV) ionization energy, respectively. Error bars denote the 1σ fitting errors. The light blue and green shades describe the result of the power-law fitting to Na I D and Mg I, respectively, with vertical 1σ fitting error range. The green and orange lines denote the best-fitting power-law function of Mg II and C II, respectively. Bottom: the central outflow velocities as a function of SFRs. The symbols are the same as those in the top panel of this figure. In both panels, the orange triangle are offset in SFR by 0.05 dex for clarity.

absorption lines, respectively, which are depicted with the diamonds in Figure 7. In the same manner as Mg I of the $z1$ -sample, we fit v_{out} (v_{max}) of Mg II by a power-law function with a slope fixed at $\alpha = 0.05$ (0.28). We obtain the best-fit parameters of $V_1 = 10^{2.21 \pm 0.01}$ ($10^{2.43 \pm 0.01}$) for $V = v_{\text{out}}$ (v_{max}). We find that v_{out} (v_{max}) at $z \sim 2$ is higher than the one at $z \sim 1$ at the 13.4σ (6.4σ) significance level. The green line in Figure 7 illustrate the best-fitting relations of Mg II at $z \sim 1$. For comparison, the orange line show the line with $\alpha = 0.05$ (0.28) through the orange diamond.

In summary, we find that v_{out} and v_{max} increase from $z \sim 0$ to 2. Although there is some implication of the redshift evolution of the outflow velocities (Du et al. 2016; Rupke et al. 2005b), this is the first time to identify the clear trend of the redshift evolution of the outflow velocities.

Here we note the effects of the selection biases. There are three sources of possible systematics that are included in our analysis. The first is the selection criterion of the SFR surface density Σ_{SFR} in the $z0$ -sample. In Section 2.1,

we select the galaxies with the criterion of Σ_{SFR} larger than $10^{-0.8} \text{ M}_{\odot} \text{ yr}^{-1} \text{ kpc}^{-2}$, but we do not apply this criterion for the $z1$ - and $z2$ -samples. A large fraction of the $z1$ -sample meets the criterion of Σ_{SFR} because the galaxies of the $z1$ -sample have the median SFR of $\sim 7 \text{ M}_{\odot} \text{ yr}^{-1}$ and the median Petrosian radius of 5.2 kpc estimated from photometry of some galaxies taken with Hubble Space Telescope/Advanced Camera for Surveys (Weiner et al. 2009). All of our $z2$ -sample also meet the criterion of Σ_{SFR} (Erb et al. 2006a). The second is the selection criterion of the inclination i in our $z0$ -sample. We select the galaxies with $i < 40^\circ$, which is less than 60° that is the typical outflow opening angle of the SDSS galaxies (Chen et al. 2010). This criterion is likely not needed for the $z1$ - and $z2$ -samples because it is reported that the outflows of the galaxies at $z \sim 1-2$ is more spherical than those at $z \sim 0$ (Weiner et al. 2009; Martin et al. 2012; Rubin et al. 2014). In addition, the galaxies under these criteria of Σ_{SFR} and i should decrease the v_{out} and v_{max} of the $z0$ -sample, indicating the redshift evolution of the outflow velocities more clearly. The third is the differences of instrumental resolutions. There is a possibility that low spectral resolutions may systematically increase the values of v_{max} . We convolve the highest resolution ($R \sim 5000$) spectra of $z1$ -sample with SDSS ($R \sim 2000$) and LRIS ($R \sim 800$) spectral resolutions and compare the v_{max} values of the original and the convolved spectra. In this way, we confirm that the systematics of the different spectral resolution is negligible in our results.

5. DISCUSSION

5.1. Mass Loading Factor

Another important parameter of the outflows is the mass loading factor η , which is defined by

$$\eta = \dot{M}_{\text{out}} / \text{SFR}, \quad (8)$$

where \dot{M}_{out} is the mass outflow rate. η represents how the outflows contribute the feedback process of the galaxy formation and evolution. We calculate η of the $z0$ -, $z1$ -, and $z2$ -samples with the absorption lines of Na I D, Mg I, and C II, respectively. Although IE (depth) of C II is higher (deeper) than Na I D and Mg I, we directly compare the values of η estimated from the absorption lines that have different IE and depths. This is because Figure 7 shows that v_{out} of Mg I and Mg II are comparable despite their different IE and depths of the absorption lines. To estimate \dot{M}_{out} , we use the spherical flow model (Rupke et al. 2002; Martin et al. 2012) that assumes the bi-conical outflow whose solid angle subtended by the outflowing gas is given by Ω . In the model, \dot{M}_{out} is given by

$$\dot{M}_{\text{out}} = \bar{m}_p \Omega C_f v_{\text{out}} R N(\text{H}), \quad (9)$$

where \bar{m}_p is mean atomic weight, R is the inner radius of the outflows, and $N(\text{H})$ is the column density of hydrogen. We can rewrite Equation (9) as

$$\dot{M}_{\text{out}} \simeq 22 C_f \text{ M}_{\odot} \text{ yr}^{-1} \times \left(\frac{N(\text{H})}{10^{20} \text{ cm}^{-2}} \right) \left(\frac{R}{5 \text{ kpc}} \right) \left(\frac{v_{\text{out}}}{300 \text{ km s}^{-1}} \right), \quad (10)$$

where we use $\bar{m}_p = 1.4 \text{ amu}$ and $\Omega = 4\pi$ that is a case of a spherical outflow. We assume that R is the same as the effective radius which are obtained in the r_e - M_* relation of Shibuya et al. (2015).

We estimate $N(\text{H})$ from the column density of an ion X^n , which is expressed as

$$N(X^n) = \frac{\tau_0 b}{1.497 \times 10^{-15} \lambda_{\text{sys}} f}, \quad (11)$$

where f is the oscillator strength. The oscillator strength is taken from Morton (1991). We define the gas-phase abundance of an element X with respect to hydrogen as $(X/\text{H})_{\text{gas}} \equiv N(X)/N(\text{H})$, where the column density of an element $N(X)$ is given by the relation

$$N(X) = \sum_n N(X^n). \quad (12)$$

$N(X^n)$ can be converted into $N(\text{H})$ with three parameters: the ionization fraction $\chi(X^n) \equiv N(X^n)/N(X)$, the dust depletion factor $d(X) \equiv (X/\text{H})_{\text{gas}}/(X/\text{H})_{\text{c}}$, and the cosmic metallicity at each redshift $\mu(X) \equiv (X/\text{H})_{\text{c}}$, where the index c refers to the cosmic average. We thus estimate $N(\text{H})$ with

$$N(\text{H}) = \frac{N(X^n)}{\chi(X^n) d(X) \mu(X)}. \quad (13)$$

It is difficult to obtain these three parameters by observations. We use the solar metallicity for $\mu(X)$ of the $z0$ -sample, and a half of the solar metallicity for $\mu(X)$ of the $z1$ - and $z2$ -samples, i.e., $\mu(X) = 0.5(X/\text{H})_{\odot}$. According to Morton (2003), the solar metallicity values are $\log(\text{Na}/\text{H})_{\odot} = -5.68$, $\log(\text{Mg}/\text{H})_{\odot} = -4.42$, and $\log(\text{C}/\text{H})_{\odot} = -3.48$. The dust depletion factors are scaled to Milky Way values taken from Savage & Sembach (1996): $d(\text{Na}) = 0.1$, $d(\text{Mg}) = 0.03$, and $d(\text{C}) = 0.4$. For the ionization fractions, we take the moderate value of $\chi(\text{Na I D}) = 0.1$, because photoionization models calculated by CLOUDY (Ferland et al. 1998, 2013) suggest $\chi(\text{Na I D}) = 10^{-4}-1$ (Murray et al. 2007; Chisholm et al. 2016). Following this choice of $\chi(\text{Na I D})$, we choose $\chi(\text{Mg I}) = 0.1$. Chisholm et al. (2016) also find $\chi(\text{Si II}) \simeq 0.2$. Because the ionization energy of Si II (16 eV) and C II (24 eV) are comparable, we assume $\chi(\text{C II}) = 0.2$ that is the same as Si II. In summary, the parameters for Na I D, Mg I, and C II are $(\chi, d, \mu) = (0.1, 0.1, 2.1 \times 10^{-6})$, $(0.1, 0.03, 1.9 \times 10^{-5})$, and $(0.2, 0.4, 1.7 \times 10^{-4})$, respectively. $N(\text{H})$ is calculated by Equation (13) with the parameter sets (χ, d, μ) .

We estimate \dot{M}_{out} by Equation (10) with C_f and v_{out} that are derived in Section 3.2, and obtain η by Equation (8). We find that our samples have $0 \lesssim \eta \lesssim 1$, which are consistent with the results of previous studies (e.g., Heckman et al. 2015). Figure 8 shows η as a function of the halo circular velocity v_{cir} . The values of v_{cir} are calculated from the stellar mass, M_* , with the M_* - M_h relation in Behroozi et al. (2013) and Equation (1) in Mo & White (2002). We perform the power-law fitting between η and v_{cir} of the $z0$ -sample, and obtain the best-fitting relation $\eta = \eta_1 v_{\text{cir}}^a$ for $\eta_1 = 17 \pm 90$ and $a = -0.5 \pm 1.1$. This scaling relation is consistent with the previous studies within the 1σ uncertainties: $a = -0.98$ for strong outflows investigated with the UV observations of the local galaxies (Heckman et al. 2015) and $a = -1.0$ for $v_{\text{cir}} > 60 \text{ km s}^{-1}$ found with the FIRE simulations (Muratov et al. 2015). Our result, $a = -0.5 \pm 1.1$, shows a weak evidence of a decreasing trend, but it is consistent with no correlation, i.e., $a = 0$. Our results are consistent with the momentum-driven model ($a = -1$). It is not conclusive, but we can rule out the energy-driven model ($a = -2$) at only the 83 percentile significance level. We also plot the data of the $z1$ - and $z2$ -samples in Figure 8, but we

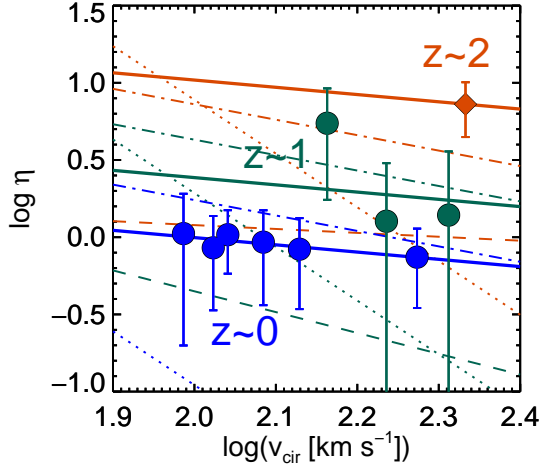


Figure 8. Mass loading factor as a function of v_{cir} . The data points are the same as those in Figure 7. The colors of blue, green, and orange correspond to $z \sim 0$, 1, and 2, respectively. The solid lines denote the linear-square fitting results. The dot-dashed, dashed, and dotted lines indicate the models presented by Muratov et al. (2015), Barai et al. (2015), and Mitra et al. (2015), respectively.

cannot discuss the scaling relation of them due to few data points.

5.2. Physical Origins of Outflow Evolution

In Section 4.2, we find that the outflow velocities increase from $z \sim 0$ to 2. This increasing trend of the outflow velocities is indicated by recent numerical simulations. Barai et al. (2015) carry out simulations with MUPPI and find that the outflow velocities increase from $z \sim 0.8$ to 3.0. Moreover, there are two studies suggesting the increasing outflow velocities towards high redshift (Oppenheimer & Davé 2008; Muratov et al. 2015) based on the following arguments. Muratov et al. (2015) conduct FIRE simulations and find the no redshift evolution of the relation between the outflow velocities and halo circular velocities at $z = 0.5$ –4.0. This no redshift evolution of the relation corresponds to the increasing trend of the outflow velocities from $z = 0.5$ to 3.0 at a fixed SFR if one assumes the M_* – M_h relation of Behroozi et al. (2013) and the SFR– M_* main sequence of Speagle et al. (2014). Similarly Oppenheimer & Davé (2008) shows the no redshift evolution of the relation between the outflow velocities and the galaxy velocity dispersion, implying that increase of the outflow velocities under the same assumptions as those above. Our results show the same trend that is predicted by these simulations above although we cannot quantitatively compare our results with those of the simulations because of the different definitions of the outflow velocity.

Our observed results in Figure 8 indicate that η increase from $z \sim 0$ to 2 at a given circular velocity. The theoretical methods also predict increase of the mass loading factors with increasing redshift. Muratov et al. (2015) obtain the simple relation $\eta \propto (1+z)^{1.3}$ that is supported by the analytic model of Hayward & Hopkins (2015). Barai et al. (2015) find the increase of η for high- M_h galaxies from $z = 0.8$ to 2.0. Moreover Mitra et al. (2015) claim that η increases with increasing redshift by $\eta \propto 10^{0.7\sqrt{z}}$ based on an analytic model with empirical relations. The dot-dashed, dashed, and dotted lines in Figure 8 show the relations predicted by Muratov et al. (2015), Barai et al. (2015), and Mitra et al. (2015), respectively. The

increase of η towards high redshift is found in these lines in Figure 8.

We fit the $z0$ -, $z1$ -, and $z2$ -samples with a power-law function $\eta = \eta_1 v_{\text{cir}}^a$ at the fixed slope of $a = -0.5$ that is the best-fit parameter of the $z0$ -sample (Section 5.1). We obtain the best-fit parameters $\eta_1 = 17 \pm 4$, 42 ± 29 , and 181 ± 70 for $z0$ -, $z1$ -, and $z2$ -samples, respectively. These relations for $z0$ -, $z1$ -, and $z2$ -samples are illustrated in Figure 8 with the blue, green, and orange solid lines, respectively. The redshift evolution of η is obtained as $\eta \propto (1+z)^{1.8 \pm 0.5}$ by a power-law fitting.

The theoretical models provide physical pictures of the increases of v_{out} , v_{max} , and η towards high redshift that are found by our observational study. Barai et al. (2015) suggest that SFRs of high-mass galaxies increase towards high redshift, and that the gas of these galaxies are rich at high redshift, which make the high values of v_{out} and η for these galaxies. Similarly, Hayward & Hopkins (2015) find that gas fractions of massive galaxies are low at $z \sim 0$, and that the value of η increases exponentially by the increase of the gas fractions towards high redshift.

We discuss the redshift evolution of the outflows, SFR, and mass of cool gas in the galaxy. If we assume that \dot{M}_{out} is proportional to cool H I gas mass $M_{\text{gas}}^{\text{cool}}$, we can write

$$\eta = \frac{\dot{M}_{\text{out}}}{\text{SFR}} \propto \frac{M_{\text{gas}}^{\text{cool}} v_{\text{out}}}{\text{SFR}}. \quad (14)$$

Hence the mass of the cool gas in the galaxy is

$$M_{\text{gas}}^{\text{cool}} \propto \frac{\eta \text{SFR}}{v_{\text{out}}}. \quad (15)$$

Below we calculate the redshift dependence of SFR, v_{out} , η , and $M_{\text{gas}}^{\text{cool}}$ at a fixed stellar mass $\log(M_*/M_\odot) = 10.5$. The redshift evolution of SFR is given by

$$\text{SFR} \propto (1+z)^{2.8} \quad (16)$$

from the results of Speagle et al. (2014). In this study, we obtain $v_{\text{out}} \propto (1+z)^{0.81 \pm 0.05} \text{SFR}^{0.05 \pm 0.04}$, fitting the power-law functions to the results of Figure 7. Substituting Equation (16), we find

$$v_{\text{out}} \propto (1+z)^{0.95 \pm 0.12}. \quad (17)$$

We also obtain $\eta \propto (1+z)^{1.8 \pm 0.5} v_{\text{cir}}^{-0.5 \pm 1.1}$, fitting the power-law functions to the results of Figure 8. If we use the relation of $v_{\text{cir}} \propto (1+z)^{0.53 \pm 0.09}$ that we estimate from the M_* – M_h relation in Behroozi et al. (2013), η is written as

$$\eta \propto (1+z)^{1.5 \pm 0.7}. \quad (18)$$

Substituting Equations (16)–(18) into Equation (15), we obtain the redshift dependence of $M_{\text{gas}}^{\text{cool}}$ by

$$M_{\text{gas}}^{\text{cool}} \propto (1+z)^{3.4 \pm 0.7}. \quad (19)$$

Equation (19) suggests that increasing $M_{\text{gas}}^{\text{cool}}$ causes the increase of outflow velocities, mass loading factors, and SFR with increasing redshift. This increasing trend of $M_{\text{gas}}^{\text{cool}}$ is consistent with independent observational results. If we assume that the molecular gas mass is proportional to $M_{\text{gas}}^{\text{cool}}$ at a given stellar mass, there is a relation of $M_{\text{gas}}^{\text{cool}} \propto (1+z)^{2.7}$ obtained by the radio observations of Genzel et al. (2015). This relation is consistent with Equation (19) within the 1σ uncertainty.

As noted in Section 5.1, however, the parameter sets used for deriving η include large uncertainties. We use the dust depletion factors estimated in the Milky Way. The ionization fractions of Na I D and Mg I may contain uncertainties of more than an order of magnitude, which linearly change the values of η (Equation 13). We thus think that the conclusion of increase of η is not strong. However, we can securely claim that the theoretical models are consistent with our observational results under the assumption of the free parameter sets shown in Section 5.1.

6. SUMMARY

We investigate redshift evolution of galactic outflows at $z \sim 0-2$ in the same stellar mass range. We use rest-frame UV and optical spectra of star-forming galaxies at $z \sim 0, 1$, and 2 taken from the SDSS DR7, the DEEP2 DR4, and Erb et al. (2006a,b), respectively. The outflows are identified with metal absorption lines: Na I D for the $z \sim 0$ galaxies; Mg I and Mg II for the $z \sim 2$ galaxies; and C II and C IV for the $z \sim 2$ galaxies. We construct composite spectra and measure the parameters of the galactic outflow properties such as the outflow velocities by the multi-component fitting with the aid of the SSP models. Our results are summarized below.

1. We find that there are the scaling relations between the outflow velocities and SFR at $z \sim 0$: for the central outflow velocity v_{out} by $v_{\text{out}} \propto \text{SFR}^{0.05 \pm 0.04}$ and for the maximum outflow velocity v_{max} by $v_{\text{max}} \propto \text{SFR}^{0.28 \pm 0.05}$. The velocities v_{out} and v_{max} are consistent with previous studies.
2. We confirm that both of the outflow velocities increase with increasing redshift. Because ions with higher ionization energy likely trace higher velocity clouds, we compare ions with the similar ionization energies: Na I D (IE $\simeq 5.1$ eV) and Mg I (IE $\simeq 7.6$ eV) from $z \sim 0$ to 1, and Mg II (IE $\simeq 15$ eV) and C II (IE $\simeq 24$ eV) from $z \sim 1$ to 2. The velocities v_{out} (v_{max}) at $z \sim 1$ is higher than those at $z \sim 0$ at the 3.0σ (4.9σ) significance level. Similarly, v_{out} (v_{max}) at $z \sim 2$ is higher than those at $z \sim 1$ at the 8.5σ (1.8σ) significance level.
3. To calculate the mass loading factors η , we use Na I D at $z \sim 0$, Mg I at $z \sim 1$, and C II at $z \sim 2$. We then find that the scaling relation between η and the halo circular velocity v_{cir} is given by $\eta \propto v_{\text{cir}}^a$ for $a = -0.5 \pm 1.1$ at $z \sim 0$. The slope of $a = -0.5 \pm 1.1$ suggests that the outflows of the SDSS galaxies are launched by a mechanism based on the momentum-driven model, which predicts $a = -1$.
4. We identify the increase of η from $z \sim 0$ to 2. The values of η increase by $\eta \propto (1+z)^{1.8 \pm 0.5}$, with the parameter sets assumed in Section 5.1. Note that the parameter sets include large uncertainties.

We find the increases of v_{out} , v_{max} , and η towards high redshift by observations. These results are consistent with theoretical predictions that explain the evolution by the increase of gas in high redshift galaxies.

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